

### 7.3: Amplitude and Vertical Shifts

“I WILL...

...identify all amplitude and vertical shifts”

#### I. Transformation of Graph Equation

A. Equation:  $y = A$  trig function  $B(x - h) + k$

B.  $A$  is the amplitude

1. Defined as how high the graph is
2. Always positive; take the absolute value
3. Also known as the scale factor
4. Only Sine and Cosine functions have amplitude

C.  $B$  is the period

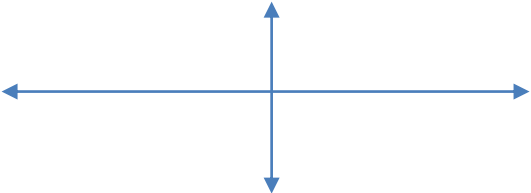
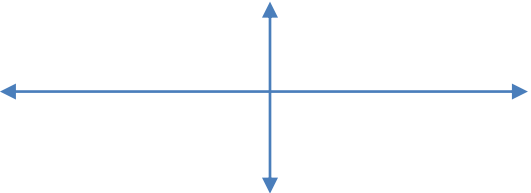
1. Period is defined as how far it goes for a full cycle
2. Frequency means the number of times you will see the graph during the regular period
3. Sine and Cosine period equation is  $\frac{2\pi}{b}$  where Tangent period equation is  $\frac{\pi}{b}$

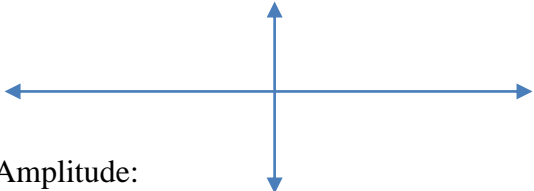
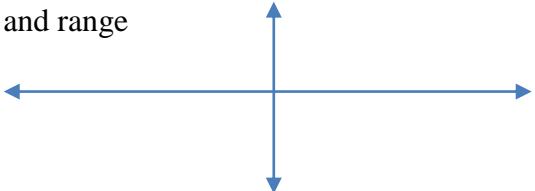
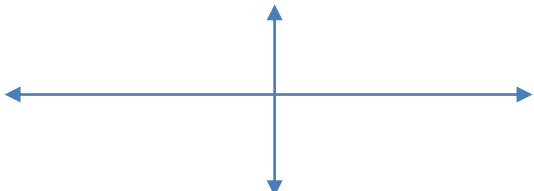
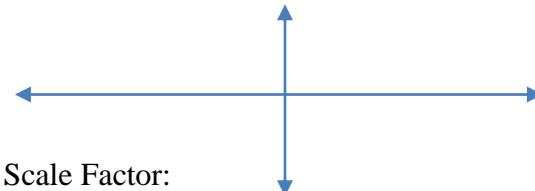
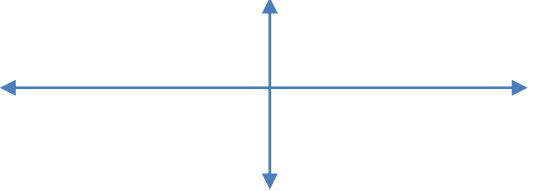
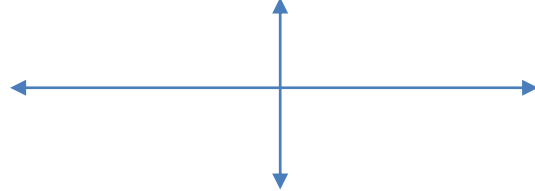
D.  $k$  is the vertical shift

1.  $+k$  is where graphs shifts up
2.  $-k$  is where graphs shifts down

#### II. Steps in Graphing

- A. Understand the parent function
- B. Determine the old points and apply the change
- C. Plot points and graph

<p>Ex 1: Graph <math>y = \sin x + 1</math> and identify amplitude, period, vertical shift, domain, and range</p>  <p>Amplitude: Period: Vertical Shift: Domain: Range:</p>	<p>Ex 2: Graph <math>y = 2\cos \theta - 1</math> and identify amplitude, period, vertical shift, phase shift, domain, and range</p>  <p>Amplitude: Period: Vertical Shift: Domain: Range:</p>
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<p>Ex 3: Graph <math>y = \frac{1}{3} \sin \frac{1}{2} t</math> from <math>[-2\pi, 2\pi]</math> and identify amplitude, period, vertical shift, domain, and range</p>  <p>Amplitude: Period: Vertical Shift: Domain: Range:</p>	<p>Your Turn: Graph <math>y = -2 \sin 4t - 1</math> from <math>[-\pi/2, \pi/2]</math> and identify amplitude, period, vertical shift, phase shift, domain, and range</p>  <p>Amplitude: Period: Vertical Shift: Domain: Range:</p>
<p>Ex 4: Graph <math>y = 2 \tan x + 1</math> from <math>[0, \pi]</math> and identify amplitude, period, vertical shift, domain, and range</p>  <p>Period: Vertical Shift: Domain: Range:</p>	<p>Ex 5: Graph <math>y = 1/2 \csc x + 1</math> from <math>[0, 2\pi]</math> and identify scale factor, period, vertical shift, domain, and range</p>  <p>Scale Factor: Period: Vertical Shift: Domain: Range:</p>
<p>Ex 6: Graph <math>y = \cot x - 2</math> from <math>[0, \pi]</math> and identify scale factor, period, vertical shift, domain, and range</p>  <p>Scale Factor: Period: Vertical Shift: Domain: Range:</p>	<p>Your Turn: Graph <math>y = -\sec x + 1</math> from <math>[0, 2\pi]</math> and identify period, vertical shift, domain, and range</p>  <p>Scale Factor: Period: Vertical Shift: Domain: Range:</p>