

### 3.8: Rewrite Formulas and Equations

“I WILL ...

Rewrite Formulas, Equations, and Functions.”

#### I. Literal Equations

- A. A literal equation is an equation that has more than one variable
- B. *Literal* in Latin means “letter.”
- C. Solve for the missing variable and substitute

#### II. Steps

- A. Move the term and variables onto one side
- B. Isolate the variable
- C. Simplify
- D. Check

#### III. Model Problems

Ex 1: Solve $ax + b = c$ for $x$ . Then, use the solution to solve, $2x + 5 = 11$ .	Ex 2: Solve $a - bx = c$ for $x$ . Then, use the solution to solve, $12 - 5x = -3$ .
Ex 3: Solve $3x + 2y = 8$ so that $y$ is a function of $x$ .	Your Turn: Solve $-2x + 3y = 6$ so that $y$ is a function of $x$ .

Ex 4: The area  $A$  of a triangle is given by the formula,  $A = 1/2bh$  where  $b$  is the base and  $h$  is the height. A) Solve for the formula of  $h$  and B) Determine the height when the area is  $64.4 \text{ meters}^2$  and the base is  $14 \text{ m}$ .

Ex 5: The perimeter  $P$  of a rectangle is given by the formula,  $P = 2l + 2w$ . A) Solve for the formula of  $w$  and B) Determine the width of the rectangle using the figure below.

$$P = 19.2 \text{ feet}$$

$$7.2 \text{ ft.}$$

Your Turn: The area  $A$  of a rectangle is given by the formula,  $A = lw$  where  $l$  is the length and  $w$  is the width. A) Solve for the formula of  $l$  and B) Determine the length when the area is  $351 \text{ cm.}^2$  and the length is  $13 \text{ cm}$ .

$$A = 351 \text{ cm.}^2$$

$$13 \text{ cm.}$$

Assignment: Pg 187: 4-30 odd

**LITERAL EQUATIONS** Solve the literal equation for  $x$ . Then use the solution to solve the specific equation.

3.  $ax = bx - c$ ;  $8x = 3x - 10$

4.  $a(x + b) = c$ ;  $2(x + 1) = 9$

5.  $c = \frac{x+a}{b}$ ;  $2 = \frac{x+5}{7}$

6.  $\frac{x}{a} = \frac{b}{c}$ ;  $\frac{x}{8} = \frac{4.5}{12}$

7.  $\frac{x}{a} + b = c$ ;  $\frac{x}{4} + 6 = 13$

8.  $ax + b = cx - d$ ;  $2x + 9 = 7x - 1$

**ERROR ANALYSIS** Describe and correct the error in solving the equation for  $x$ .

9.  $ax + b = 0$   
 $ax = b$   
 $x = \frac{b}{a}$

10.  $c = ax - bx$   
 $c = (a - b)x$   
 $c(a - b) = x$

**REWRITING EQUATIONS** Write the equation so that  $y$  is a function of  $x$ .

11.  $2x + y = 7$

12.  $5x + 4y = 10$

13.  $12 = 9x + 3y$

14.  $18x - 2y = 26$

15.  $14 = 7y - 6x$

16.  $8x - 8y = 5$

17.  $30 = 9x - 5y$

18.  $3 + 6x = 11 - 4y$

19.  $2 + 6y = 3x + 4$

**REWRITING FORMULAS** Solve the formula for the indicated variable.

20. Volume of a rectangular prism:  $V = \ell wh$ . Solve for  $w$ .

21. Surface area of a prism:  $S = 2B + Ph$ . Solve for  $h$ .

22. Length of movie projected at 24 frames per second:  $\ell = 24f$ . Solve for  $f$ .



23. **TAKS REASONING** The formula for the area of a trapezoid is

$A = \frac{1}{2}(b_1 + b_2)h$ . Which equation is *not* equivalent to the formula?

- (A)  $h = \frac{2A}{b_1 + b_2}$     (B)  $b_1 = \frac{2A}{h} - b_2$     (C)  $b_2 = \frac{2A}{b_1} - h$     (D)  $b_2 = \frac{2A}{h} - b_1$

**REWRITING EQUATIONS** Write the equation so that  $y$  is a function of  $x$ .

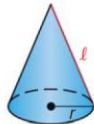
24.  $4.2x - 2y = 16.8$

25.  $9 - 0.5y = 2.5x$

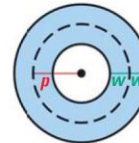
26.  $8x - 5x + 21 = 36 - 6y$

**GEOMETRY** Solve the formula for the indicated variable. Then evaluate the rewritten formula for the given values. (Use 3.14 for  $\pi$ .)

27. Surface area of a cone:  
 $S = \pi r \ell + \pi r^2$ .  
Solve for  $\ell$ . Find  $\ell$  when  
 $S = 283 \text{ cm}^2$  and  $r = 5 \text{ cm}$ .



28. Area of a circular ring:  
 $A = 4\pi pw$ .  
Solve for  $p$ . Find  $p$  when  
 $A = 905 \text{ ft}^2$  and  $w = 9 \text{ ft}$ .



29. **TAKS REASONING** Describe a real-world situation where you would want to solve the distance traveled formula  $d = rt$  for  $t$ .

**CHALLENGE** Solve the literal equation for  $a$ .

30.  $x = \frac{a+b+c}{ab}$

31.  $y = x \left( \frac{ab}{a-b} \right)$