

3-2A: Angles Formed by Parallel Lines and Transversals

“I WILL ...

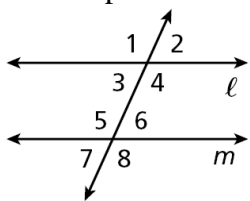
...prove and use theorems about the angles formed.”

I. Definitions

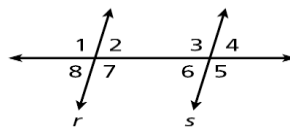
- A. \_\_\_\_\_ describes a fundamental relationship between the basic terms of geometry: Accepted to be true without proof
- B. \_\_\_\_\_: A statement or conjecture that can be proven true by undefined terms, definitions and postulates.

Type of Theorem/Postulate	Definition	Visual Example
Converse of the Corresponding Angle Postulate	If two coplanar lines are cut by a transversal, so that a pair of corresponding angles are congruent, then the two lines are parallel	
Parallel Postulate	Through a point $P$ and not on the line $\ell$ , there is exactly one line parallel to $\ell$ .	
Converse of the Alternate Interior Theorem	If two coplanar lines are cut by a transversal so that a pair of alt. interior angles are congruent, then the two lines are parallel.	
Converse of the Alternate Exterior Angles Theorem	If two coplanar lines are cut by a transversal so that a pair of alt. ext. angles are congruent, then the two lines are parallel.	
Converse of Same-Side Interior Angles Theorem	If two coplanar lines are cut by a transversal so that a pair of alt. same-side interior angles are supplementary, then the two lines are parallel.	

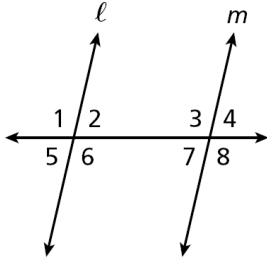
Ex 1: Use the Converse of the Corresponding Angles Postulate and the given information to show that  $\ell \parallel m$  given  $m\angle 3 = (4x - 80)^\circ$ ,  $m\angle 7 = (3x - 50)^\circ$ ,  $x = 30$  and convert it to a two-column proof



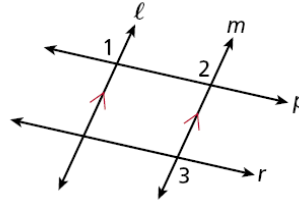
Ex 2: Use the Converse of the Corresponding Angles Postulate and the given information to show that  $r \parallel s$  given  $m\angle 2 = (10x + 8)^\circ$ ,  $m\angle 3 = (25x - 3)^\circ$ ,  $x = 5$  and convert it to a two-column proof



Your Turn: Use the Converse of the Corresponding Angles Postulate and the given information to show that  $\ell \parallel m$  given  $m\angle 7 = (4x + 25)^\circ$ ,  $m\angle 5 = (5x + 12)^\circ$ ,  $x = 13$  and convert it to a two-column proof

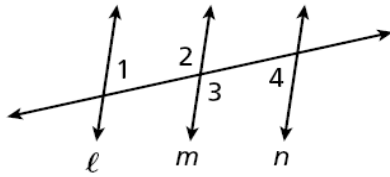


Ex 3: Using the diagram below, solve for  $m\angle EDG$  and  $m\angle BDG$



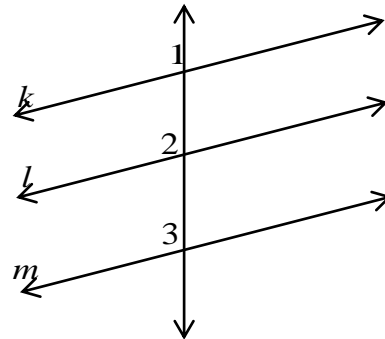
Statements	Reasons
1) $p \parallel r$	Given
2)	
3) $\angle 1 \cong \angle 3$	Given
4)	
5) $l \parallel m$	

Ex 4: Given:  $\angle 1 \cong \angle 4$ ,  $\angle 3$  and  $\angle 4$  are supplementary.  
Prove:  $\ell \parallel m$

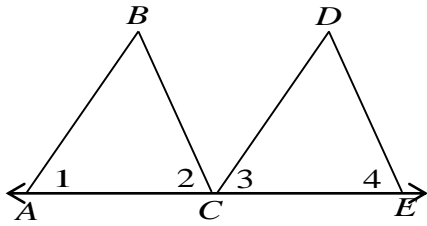


Statements	Reasons
1) $\angle 1 \cong \angle 4$	Given
2)	Def'n of Congruency
3) $\angle 3$ and $\angle 4$ are supplementary	Given
4)	
5)	
6)	
7) $m\angle 2 + m\angle 1 = 180^\circ$	
8) $\ell \parallel m$	

Ex 5: Given:  $\ell \parallel k$  and  $m \parallel k$   
Prove:  $\ell \parallel m$



Your Turn: Given:  $\overline{AB} \parallel \overline{CD}$ ,  $\angle 1 \cong \angle 2$ ,  $\angle 3 \cong \angle 4$   
Prove:  $\overline{BC} \parallel \overline{DE}$



Assignment: Pg. 166: 15, 19-21, 24-36 all