

## 2.2: Finding Slope and Rate of Change

“I WILL ...

Apply the slope equation to find the rate of change.”

### I. Definitions

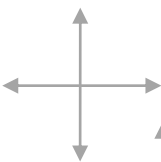
- A. Linear equation: An equation whose graph is a line
- B. Slope is a non-vertical line of the vertical change to the horizontal change between two points of a line
- C. Y-intercept is where the line crosses the *y-axis*

### II. Slope

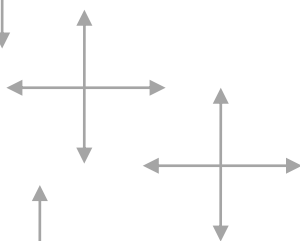
- A. Slope Equation is  $m = \frac{y_2 - y_1}{x_2 - x_1}$
- B. Rewrite the equation as  $\frac{\Delta y}{\Delta x} = \frac{\text{rise}}{\text{run}}$
- C. Rise: The number of points up (vertically) from the previous point
- D. Run: The number of points sideways (horizontally) from the rise

### III. Types of Slope

A. Positive Slope:



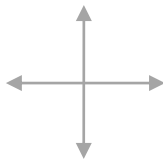
B. Negative Slope:



C. Zero Slope:



D. Undefined Slope:



E. Zero vs. Undefined “Heaven over Hell.”

### IV. Steps

- A. Find the change of *Y* and change of *X* of two of the points
- B. Determine the ratios for both
- C. Simplify the ratio
- D. Repeat the process for two other points
- E. Check answer

V. Model Problems

<p>Ex 1: What is the slope of these two points, <math>(-1, 3)</math> and <math>(2, -2)</math>? Will it rise, fall, horizontal, or vertical?</p>	<p>Your Turn: What is the slope of this table? Will it rise, fall, horizontal, or vertical?</p> <table border="1" data-bbox="824 331 1382 422"> <tr> <td><math>x</math></td> <td>-2</td> <td>0</td> <td>2</td> <td>4</td> </tr> <tr> <td><math>f(x)</math></td> <td>2</td> <td>1</td> <td>0</td> <td>-1</td> </tr> </table>		$x$	-2	0	2	4	$f(x)$	2	1	0	-1
$x$	-2	0	2	4								
$f(x)$	2	1	0	-1								
<p>Ex 2: What is the slope of this table? Will it rise, fall, horizontal, or vertical?</p> <table border="1" data-bbox="240 810 797 898"> <tr> <td><math>x</math></td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td><math>f(x)</math></td> <td>2</td> <td>4</td> <td>8</td> <td>16</td> </tr> </table>	$x$	2	3	4	5	$f(x)$	2	4	8	16	<p>Your Turn: What is the slope of these two points, <math>(1, -5)</math> and <math>(1, 0)</math>? Will it rise, fall, horizontal, or vertical?</p>	
$x$	2	3	4	5								
$f(x)$	2	4	8	16								
<p>Ex 3: What is the slope of these two points, <math>f(2) = 2</math> and <math>f(6) = 8</math>? Will it rise, fall, horizontal, or vertical?</p>	<p>Ex 4: What is the slope of these two points, <math>f(a) = 3</math> and <math>f(-2a) = 7</math>?</p>	<p>Your Turn: What is the slope of these two points, <math>f(2) = 8</math> and <math>f(6) = 8</math>? Will it rise, fall, horizontal, or vertical?</p>										

Assignment: Page 86: 3-17 odd, 29-33 odd


**FINDING SLOPE** Find the slope of the line passing through the given points.  
Then tell whether the line *rises, falls, is horizontal, or is vertical*.

- |                      |                      |                       |
|----------------------|----------------------|-----------------------|
| 3. (2, -4), (4, -1)  | 4. (8, 9), (-4, 3)   | 5. (5, 1), (8, -4)    |
| 6. (-3, -2), (3, -2) | 7. (-1, 4), (1, -4)  | 8. (-6, 5), (-6, -5)  |
| 9. (-5, -4), (-1, 3) | 10. (-3, 6), (-7, 3) | 11. (4, 4), (4, 9)    |
| 12. (5, 5), (7, 3)   | 13. (0, -3), (4, -3) | 14. (1, -1), (-1, -4) |


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**ERROR ANALYSIS** Describe and correct the error in finding the slope of the line passing through the given points.

15.

$$\begin{array}{l} (-4, -3), (2, -1) \\ m = \frac{-1 - (-3)}{-4 - 2} = -\frac{1}{3} \end{array}$$


16.

$$\begin{array}{l} (-1, 4), (5, 1) \\ m = \frac{5 - (-1)}{1 - 4} = -2 \end{array}$$


17.  **TAKS REASONING** What is true about the line through (2, -4) and (5, 1)?

- |  |  |
|--|--|
| <input type="radio"/> (A) It rises from left to right. | <input type="radio"/> (B) It falls from left to right. |
| <input type="radio"/> (C) It is horizontal.            | <input type="radio"/> (D) It is vertical.              |

**FINDING SLOPE** Find the slope of the line passing through the given points.

- |   |   |   |
|---|---|---|
| 29. $(-1, \frac{3}{2}), (0, \frac{7}{2})$ | 30. $(-\frac{3}{4}, -2), (\frac{5}{4}, -3)$ | 31. $(-\frac{1}{2}, \frac{5}{2}), (\frac{5}{2}, 3)$ |
| 32. (-4.2, 0.1), (-3.2, 0.1)              | 33. (-0.3, 2.2), (1.7, -0.8)                | 34. (3.5, -2), (4.5, 0.5)                           |